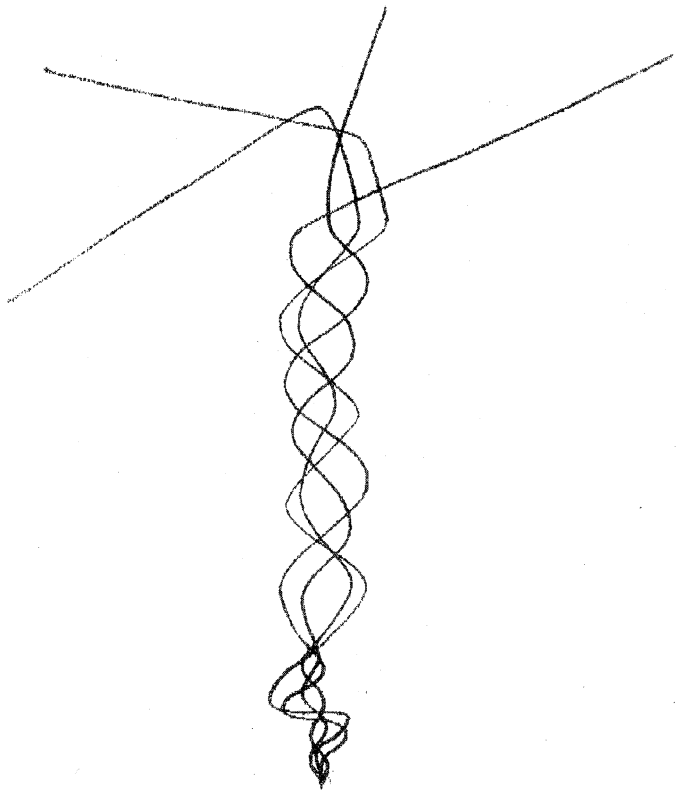
SIMULTANEOUS COMPONENT AND FACTOR ANALYSIS METHODS FOR TWO OR MORE GROUPS: A COMPARATIVE STUDY

Jan Niesing



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Jan Niesing

DEPARTMENT OF PSYCHOLOGIE
University of Groningen

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CONTENTS

CHAPTER 1 GENERALIZED COMPONENTS ANALYSIS

1.1	Introduction	1
1.2	Principal Components Analysis	2
1.3	Comparing the Varimax rotated components	5
1.4	Applying the Generalized Procrustes Rotation	6
1.5	Methods for simultaneous analysis in two or more groups, used in the present study	7
1.6	Goals of the present study	9
1.7	Other methods for the simultaneous analysis in two or more groups: IDIOSCAL, PARAFAC2 and INDSCAL	10
1.7.1	Multidimensional Scaling	11
1.7.2	IDIOSCAL	11
1.7.3	PARAFAC2	12
1.7.4	INDSCAL	14
1.7.5	Reasons for not selecting the MDS methods	15
1.8	Discarding the Partial Common Principal Components method	15
1.8.1	Partial Common Principal Components (PCPC)	15
1.8.2	Reasons for discarding PCPC	16
1.9	Factor Analysis versus Components Analysis in the one group situation	18
1.10	The organization of the present study	21

CHAPTER 2 THE METHODS UNDER INVESTIGATION

2.1	Introduction	23

2.2	Simultaneous Components Analysis methods	23
2.2.1	SCA–W	24
2.2.2	SCA–P	25
2.2.3	SCA–S	26
2.3	A Simultaneous Factor Analysis method	26
2.3.1	Simultaneous Factor Analysis in Several Populations, using a Maximum Likelihood estimation procedure (SIFASP–ML)	26
2.3.2	Identification of parameters	28
2.4	Rotations used to facilitate interpretation of the solutions, found with the methods of analysis	29
2.4.1	HKIC Rotation of the SCA–P and the SIFASP–ML solution	30
2.4.2	Hakstian's Rotation of the SCA–W solution	31
2.4.3	Simple Structure Rotation of the SCA–S solution	31
2.5	Measures of fit for the SCA methods and SIFASP–ML	32
2.5.1	Explained variances of the SCA–W solutions	32
2.5.2	Explained variances of the SCA–P solutions	33
2.5.3	Explained variances of the SCA–S solutions	33
2.5.4	The Chi–Square measure for SIFASP–ML	34
2.6	First comparison of the methods	34
2.6.1	Comparisons of PCA–sep, SCA–W, SCA–P and SCA–S	34
2.6.2	Comparison of the SCA–methods with SIFASP–ML	35

CHAPTER 3 CONSTRUCTING DATA WITH KNOWN FACTOR STRUCTURE

3.1	Introduction	37
3.1.1	Terminology	37
3.2	Description of the data construction	38
3.2.1	Choosing a true pattern matrix $\mathbf{P}_{tk}$ and defining a true structure matrix $\mathbf{S}_{tk}$ when simulating a correlation or a covariance matrix	39
3.2.2	The non–uniqueness of the true weights matrix $\mathbf{W}_{tk}$	41
3.3	Definition of data categories	42
3.3.1	Sampling from one population	43

3.3.2 Sampling from two or more populations 43
3.3.3 Explained variances in the populations 44
3.4 A measure for the similarity of populations 46
3.4.1 The Congruence Measure 46

CHAPTER 4 INDEPENDENT VARIABLES, DIMENSION INDICATORS AND SUCCESS CRITERIA

4.1 Manipulations 49
4.1.1 Independent Variables 49
4.1.2 The true matrices underlying the constructed data 51
4.2 Dimension indicators for the SCA–methods 53
4.2.1 Additional value greater than one (KA1) 53
4.2.2 Parallel Analysis (PA) 54
4.2.3 The Quotient of Additional values (QA) 55
4.2.4 The Quotient of Differences in Additional values (QDA) 57
4.2.5 The use of the dimension indicators in the present study 58
4.3 Dimension indicators for the method SIFASP–ML 59
4.3.1 The Chi–square statistic 61
4.3.2 The Sequential Chi–square Difference Test (SCDT) 62
4.3.3 Root Mean Square Error of Approximation (RMSEA) 63
4.3.4 Expected Cross–Validation Index (ECVI) 65
4.3.5 Check of fit indices for the model with the correct dimension 67
4.3.6 The use of the fit indices as dimension indicators in the present study 67
4.3.7 Checks on the solutions of LISREL 8 68
4.4 Success Criteria 69
4.4.1 The Recovery Rate (RR) 69
4.4.2 The Difference in Factor correlations (DFC) 70
4.4.3 Additional criteria for the SCA–methods: Amounts of explained variance 70
4.5 Pilot experiment to determine the preferable range of noise to signal ratios for constructed data, using the SCA–methods 71

4.5.1	Data	71
4.5.2	Measures	72
4.5.3	Results	73
4.5.4	Conclusion about meaningful noise levels	75
4.6	Pilot experiment to determine the preferable convergence value for the iterative procedures in the methods SCA-W and SCA-S	75
4.6.1	Data	76
4.6.2	Measures	76
4.6.3	Results	77
4.6.4	Conclusion about meaningful convergence criteria	77

CHAPTER 5 EXPERIMENT 1, FIRST COMPARISON OF THE THREE SCA-METHODS

5.1	Introduction	79
5.2	Manipulations of the data	79
5.2.1	One-population data	80
5.2.2	Two-or-more-populations data	81
5.3	Dependent Variables	81
5.4	Analysis	83
5.5	Questions to be answered by this experiment	85
5.6	Results	86
5.6.1	Finding the preferable dimension indicator	87
5.6.2	Finding the SCA-method with the best dimension indication	91
5.6.3	Finding the SCA-method with the best recovery of factors	96
5.6.3.1	Samples from one population	101
5.6.3.2	Samples from two populations	103
5.6.4	Finding the SCA-method with the best recovery of correlations between factors	108
5.6.5	Discerning the 'samples from one population' from the 'samples from two populations' condition	110
5.6.6	Recovery of factors for specific cases of samples from one population	115

5.7 Conclusion 118

CHAPTER 6 EXPERIMENT 2, TESTING THE METHOD SIFASP-ML

6.1 Introduction 121
6.2 Manipulations of the data 121
6.3 Dependent Variables 122
6.4 Analysis 122
6.5 Questions to be answered by this experiment 124
6.6 Results 124
6.6.1 Finding the preferable dimension indicator for SIFASP-ML 125
6.6.2 Determining the method with the best recovery of factors 132
6.6.2.1 Samples from one population 133
6.6.2.2 Samples from two populations 135
6.6.3 Determining the method with the best recovery of correlations between factors 137
6.6.4 Frequency of bad fit for the solution with the correct dimension 139
6.7 Conclusion 141

CHAPTER 7 EXPERIMENT 3, COMPARISON OF THE SCA-METHODS, WHEN THE STRENGTH OF FACTORS WITH THE SAME INTERPRETATION DIFFERS ACROSS GROUPS

7.1 Introduction 143
7.2 Manipulations of the data 143
7.3 Dependent Variables 145
7.3.1 A problem with the method SCA-S in some of the conditions studied 145
7.3.2 A measure used for inspecting whether the relative strength of the recovered factors resembles the relative strength of the true factors: the Quotient of Component Strengths (QCS) 147

7.4	Analysis	148
7.5	Questions to be answered by this experiment	148
7.6	Results Experiment 3a	149
7.6.1	Finding the SCA-method with the best dimension indication	150
7.6.2	Finding the SCA-method with the best recovery of factors	152
7.6.3	Finding the SCA-method with the best recovery of the relative strength of factors	154
7.6.4	Finding the SCA-method with the best recovery of correlations between factors	157
7.7	Results Experiment 3b	159
7.7.1	Finding the SCA-method with the best dimension indication	159
7.7.2	Finding the SCA-method with the best recovery of factors	159
7.7.3	Finding the SCA-method with the best recovery of the relative strength of factors	160
7.7.4	Finding the SCA-method with the best recovery of correlation between factors	162
7.8	Conclusion	162

CHAPTER 8 EXPERIMENT 4, COMPARISON OF THE SCA-METHODS AND SIFASP-ML-C, FOR VARIOUS CONDITIONS

8.1	Introduction	165
8.2	Manipulations of the data	165
8.3	Dependent Variables	166
8.4	Analysis	167
8.5	Questions to be answered by this experiment	167
8.6	Results Experiment 4	168
8.6.1	Experiment 4a: Four groups	168
8.6.2	Experiment 4b: Samples of n=300, n=500 and n=1000	169
8.6.3	Experiment 4c: Overlapping factors	172
8.7	Conclusion	173

CHAPTER 9 CONCLUSION AND DISCUSSION

9.1	Overview of the results and discussion	175
9.1.1	The preferable method: SCA–P	175
9.1.2	Characteristics of the methods SCA–S, SCA–W and SIFASP–ML	177
9.1.3	Results for the dimension indicators	179
9.1.4	The discriminant function for discerning samples from one population from samples from two populations	181
9.2	Limitations of the present study	182
9.2.1	Beyond the values of the independent variables	182
9.2.2	Data simulation	183
9.2.3	Methods and rotations	184
9.3	User friendliness of the programs used	184
9.4	Guidelines when analyzing data from two or more groups	186

Appendix A	True pattern matrices (of order 12×2 and 12×4) used in this study	189
Appendix B	Identification constraints used for the LISREL program	192
Appendix C	Deriving the largest possible difference in explained variance between the methods SCA–W and SCA–P in case two rank q matrices are analyzed	194
Appendix D	Examining real life data	195
	D.1 Meredith (1964) data	195
	D.2 Van Schuur (1984) data	199

References 205

Summary (in Dutch) 211

Author index 217